

Supplementary Material for: A Survey on Hypergraph Representation Learning

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A METHODOLOGY

This section clarifies the data collection process and the inclusion criteria for the selected articles.

A.1 Data Collection

We conducted our literature review by in-depth reading, interpreting, and categorizing articles addressing the problem of generating a low-dimensional representation of a hypergraph. We carried out our search in the Scopus database since it represents a comprehensive and accurate database of peer-reviewed research articles in the fields relevant to this survey. Specifically, we submitted the following query: TITLE-ABS-KEY (“hypergraph embedding” OR “hypergraph learning” OR “hypergraph representation learning” OR “hypergraph neural network*” OR “hypergraph convolution” OR “hypergraph attention”), limiting the results to only English-written contributions. We repeated the same query by replacing the word hypergraph with the terms hyper-network and high-order, as well as trying out different spellings of these words. We did not limit either the subject areas or the publication year. The rationale behind this choice relies on two main reasons. First, hypergraphs—and, more generally, graphs—embody a tool to study emergent phenomena in a wide range of application domains. Second, hypergraphs rose to prominence only recently in the academic landscape, and the topic of hypergraph representation learning represents an even more novel research field. A total of 1,338 non-duplicated articles met these criteria by June 2022.

A.2 Inclusion Criteria

We followed a standard two-step selection process to pick the final set of articles to include in this survey. First, we screened the original set by filtering each article based on its title and abstract. In this phase, we removed all articles related to (higher) student education and high-order neural networks [64, 86]. In the second step, we filtered the remaining articles based on their content, removing out-of-scope articles, such as hypergraph-regularized methods. After this process, the number of articles was narrowed down to 102. Figure 1 schematically shows the selection process, while Figure 2 provides an overview of the venues where the selected articles have been published.

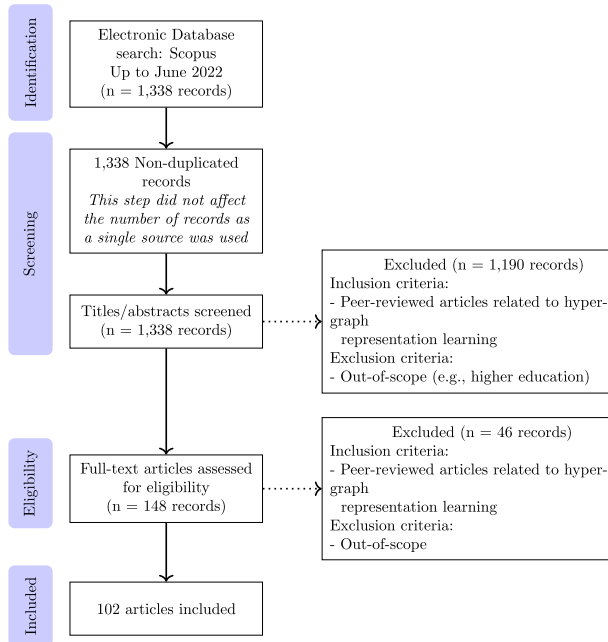


Fig. 1. PRISMA chart reporting the selection process of our systematic literature review.

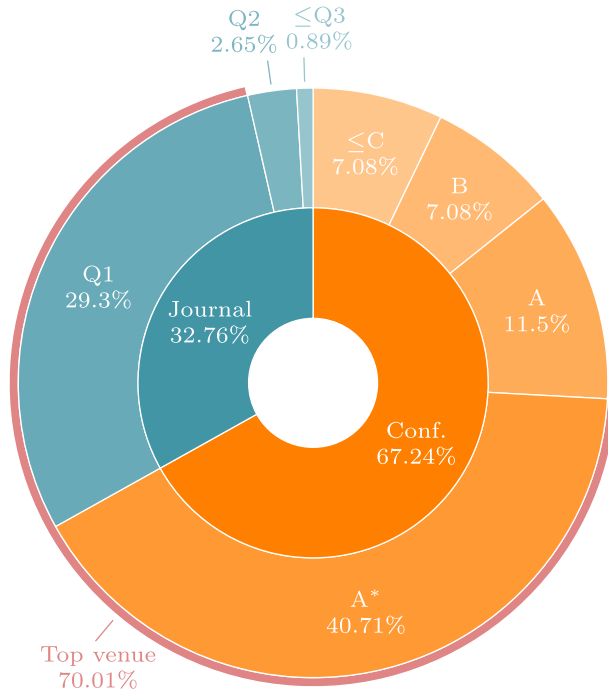


Fig. 2. Distribution of the ranking of the venues where the selected articles have been published. Conference and journal rankings have been evaluated according to **CORE 2021** (A* > A > B > C > not ranked) and **Scimago** (Q1 > Q2 > Q3 > Q4), respectively.

B INPUT SETTING

B.1 Types of Input Hypergraphs

Figure 3 shows different examples of possible input hypergraphs.

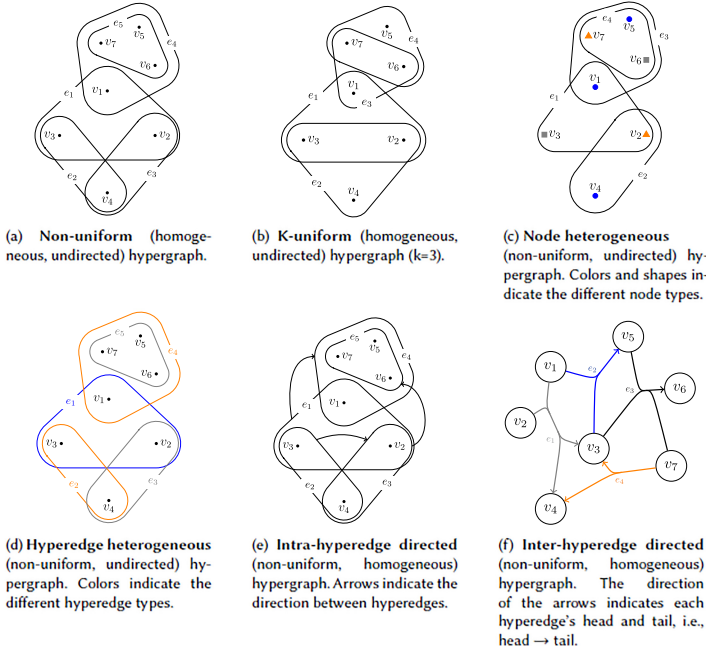


Fig. 3. Types of input hypergraphs. An example of a dynamic hypergraph is not shown because it is usually represented as a sequence of static hypergraphs.

C HYPERGRAPH REPRESENTATION LEARNING METHODS

C.1 Input Settings

In this survey, we analyze the hypergraph embedding input along six axes: the nature of the high-order relation, its directionality, and size, the temporal dimension, whether nodes have attached additional information, and whether the hypergraph is converted into a graph. Figure 4 outlines the considered input settings.

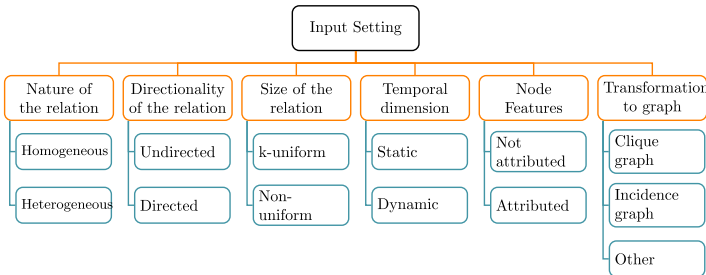


Fig. 4. Taxonomy of input settings.

C.2 Taxonomy of Hypergraph Embedding Methods

We divide hypergraph embedding techniques into three macro categories: spectral learning methods, proximity preserving methods, and (deep) neural networks-based methods. Figure 5 summarizes this taxonomy.

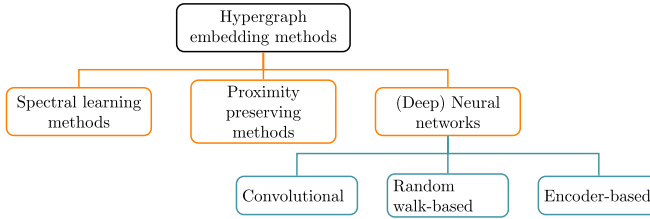


Fig. 5. Taxonomy of hypergraph embedding methods.

C.3 Temporal Distribution of the Literature about Hypergraph Embedding

Figure 6 provides the temporal distribution of the articles covered in this survey divided according to their category. The overall number of works from 2022 takes into account only the articles published by June of the same year (see Section A). Spectral learning methods were the first to appear in the literature (i.e., from the 1990s). Although the works before 2008 were primarily theoretical and did not strictly focus on learning hypergraph representations as we mean nowadays, their theoretical findings were essential to developing the most recent approaches. Besides rare exceptions traditionally linked to visualization tasks, spectral learning techniques fail when facing large-scale hypergraphs. This drawback should explain their disappearance in recent years. A different consideration must be made for the proximity-preserving family. While spectral learning methods are more mathematics-driven, we can consider proximity-preserving techniques to be more machine learning-driven as they follow the usual machine learning pipeline. However, the researchers' interest in these methods started when **deep neural networks (DNNs)** were already a big deal and, as for machine learning research in general, DNNs have stolen the show. The rise of DNN techniques began right after the introduction of Graph Convolutional Networks by Kipf and Welling in 2017 [63]. Over the past few years, the increase in computational power and experience working with graph convolutions has allowed a rapid escalation of DNN methods, currently representing the de facto technique for hypergraph representation learning.

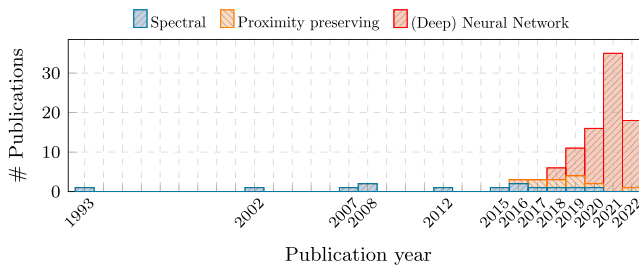


Fig. 6. Temporal distribution of the articles considered in this survey.

D SPECTRAL REPRESENTATION LEARNING METHODS

Table 1 provides an overview of the spectral methods described in the survey.

Table 1. Spectral-based Methods

Method	Input HG	Laplacian = $Z(D_{\mathcal{V}} - S_{\mathcal{V}})Z^T$	Learning Task	Venue	Year
Bolla [10]	Hom, NU	$S_e = D_e^{-1}$ and $Z = I_{ V }$	-	Discrete Mathematics	1993
Rodriguez [92]	Hom, NU	$D_r = \text{diag}(HWH^T - D_{\mathcal{V}})$, $Z = D_r^{-1/2}$, $S_e = W$, $S_{\mathcal{V}} = HS_eH^T - D_r$	-	Linear & Multilinear Algebra	2002
Zhou et al. [149]	Hom, NU	$S_e = WD_e^{-1}$ and $Z = D_{\mathcal{V}}^{-1/2}$	Clustering	NeurIPS	2007
Ren et al. [91]	Hom, NU	$S_e = \frac{1}{2}I_{ E }$ and $Z = \sqrt{2}I_{ V }$	Clustering	SSPR	2008
Sun et al. [103]	Hom, NU, A	Zhou's Laplacian	Classification	KDD	2008
Pu and Faltings [90]	Hom, NU	$S_e = W$ and $Z = D_{\mathcal{V}}^{-1/2}$ (*)	Classification	ECML PKDD	2012
Yuan and Tang [144]	Hom, NU, A	Zhou's Laplacian (*)	Classification	IEEE GRSL	2015
Zhu et al. [150]	Het, NU	$Z = I_{ V }$ and $S_e = WD_e^{-1}$	Recommendation	Neurocomputing	2016
Huang et al. [53]	Het, NU, A	Zhou's Laplacian (*)	Dimensionality reduction	Neurocomputing	2016
Sun et al. [107]	Hom, NU, A	$Z = I_{ V }$ and $S_e = WD_e^{-1}$	Classification	Remote Sensing	2017
Saito et al. [94]	Hom, NU	$Z = D_{\mathcal{V}}^{-1/2}$, $S_e = D_e^{-1}W$, $S_{\mathcal{V}} = A - \text{diag}(A)$, $A = HS_eH^T$	Clustering	AAAI	2018
Luo et al. [73]	Hom, NU, A	Zhou's Laplacian (*)	Classification	IEEE Trans. on Cybernetics	2019
Luo et al. [74]	Hom, NU, A	Zhou's Laplacian (*)	Classification	JSTARS	2020

As tasks, we only consider those directly using the node embeddings (standard output among these methods). All methods are transductive and work in a static and undirected input setting. Hom/Het stand for homogeneous/heterogeneous; NU stands for non-uniform; A stands for attributed nodes. (*) The formulation is related but does not directly fit the framework (3).

E PROXIMITY-PRESERVING METHODS

Table 2 summarizes the proximity-preserving methods described in the survey.

Table 2. Proximity-Preserving Methods

Method	Input HG	Proximity Model	Learning Task	Venue	Year	Code
HEBE [40]	Het, NU	Softmax of the dot-product	Classification	ICDM	2016	https://bitbucket.org/hgui/hebe/downloads/
HEBE-PO [41]	Het, NU	As HEBE	Classification	TKDE	2017	https://bitbucket.org/hgui/hebe/downloads/
HEBE-PE [41]	Het, NU	As HEBE	Link prediction	TKDE	2017	https://bitbucket.org/hgui/hebe/downloads/
HGE [141]	Het, NU	Multilinear map	Recommendation	CIKM	2018	https://github.com/chia-an/HGE
Event2vec [22]	Het, NU	Sigmoid of the weighted dot-product	Clustering, Class.	ICDMW	2018	-
FOBE [108]	Hom, NU	Sigmoid of the dot-product	Link prediction, Recom.	MLG	2019	https://github.com/JSybrandt/HypergraphEmbedding
HOBE [108]	Hom, NU	ReLU of the dot-product	Link prediction, Recom.	MLG	2019	https://github.com/JSybrandt/HypergraphEmbedding
LBSN2Vec [137]	Het, U	Cosine similarity	Link prediction, Recom.	WWW	2019	https://github.com/eXascaleInfolab/LBSN2Vec
LBSN2Vec++ [138]	Het, U	Cosine similarity	Link prediction, Recom.	TKDE	2020	https://github.com/eXascaleInfolab/LBSN2Vec
MSC-LBSN [111]	Het, U	Cosine similarity	Link prediction, Recom.	TKDE	2022	-

Node embedding is the standard output. All methods are transductive and work in a static and undirected input setting. Hom/Het stand for homogeneous/heterogeneous; (N)U stands for (non-)uniform. Task: Class stands for classification, and Recom for recommendation.

F (DEEP) NEURAL NETWORKS MODELS

Table 3 summarizes the (deep) neural-network-based methods described in the survey.

Table 3. (Deep) Neural Network Methods

Method	Input HG	Embedding Output	MPF	Skip-conn	Attention	Gated upl	Spectral	RW	Enc-based	Task	Venue	Year	Code (github.com/)
DHNE [112]	Het, U	✓							✓	Class, LP	AAAI	2018	tadpole/DHNE
DHNE [21]	Het, NU	✓						✓		Class, LP	ICME	2018	-
HHNE [5]	Het, NU	✓	✓	✓						LP	ICDM	2018	ilidanlab/HHNE
HGNN [33]	Hom, NU	✓	✓	✓						Class	AAAI	2019	iMoonLab/HGNN
Hyper2Vec [48]	Hom, NU	✓						✓		Class	DASFAA	2019	jeffhj/NHNE
DHGNN [56]	Hom, NU	✓	✓							Class	IJCAI	2019	iMoonLab/DHGNN
HpLapGCN [35]	Hom, NU	✓					✓			Class	Neurocom.	2019	-
Hyper-gram [51]	Het, U	✓						✓		LP	CIKM	2019	HKUST-KnowComp/HPHG
HyperGCN [134]	Hom, NU	✓	✓							Class	NeurIPS	2019	mallabise/HyperGCN
DHE [87]	Hom, NU, MC	✓, &						✓	✓	Class	NeurIPS	2019	Josh-Payne/deep-hyperedges
Hyper-SAGNN [147]	Het, NU	✓			✓			✓	✓	LP	ICLR	2020	ma-complio/Hyper-SAGNN
HyperRec [118]	Het, NU, D	✓	✓	✓		✓				Recom	SIGIR	2020	-
NHNE [47]	Hom, NU, MC	✓, &						✓		Class, LP	TOIS	2020	jeffhj/NHNE
HNHN [28]	Hom, NU	✓, &	✓							Class	ICMLW	2020	-
MGCN [15]	Hom, NU	✓	✓	✓						LP	KDD	2020	-
DHCF [54]	Hom, NU, MC	✓	✓	✓						Recom	KDD	2020	-
HGC-RNN [140]	Hom, NU	✓	✓		✓	✓				Regr	KDD	2020	-
NHP [135]	Het, NU, Dir	✓	✓							LP	CIKM	2020	-
AdaHGNN [126]	Hom, NU	✓	✓							Class	MM	2020	-
HyperGAT [26]	Het, NU, MC	✓, &	✓		✓					Class	EMNLP	2020	kaize0409/HyperGAT
SHCN [17]	Het, U	✓	✓	✓						Recom	TOIS	2020	-
G-MPNN [133]	Hom, NU	✓	✓							Class, LP	NeurIPS	2020	naganandy/G-MPNN-R
HGAT [13]	Hom, NU	✓	✓							Class	TrustCom	2020	-
HAIN [3]	Hom, NU	✓	✓	✓						Class	IEEE BigData	2020	-
HCR [55]	Het, NU	✓	✓	✓						Recom	ICDM	2021	-
HCHA [2]	Hom, NU	✓	✓	✓	✓					Class	Pat Rec	2021	-
DHCN [131]	Hom, NU	✓	✓	✓						Recom	AAAI	2021	xiaxin1998/DHCN
HWNN [104]	Het, NU, MC	✓	✓				✓			Class	WSDM	2021	-
STHGNN [121]	Hom, NU, D, MC	✓	✓			✓				Regr	TITS	2021	-
HGCELM [72]	Hom, NU	✓	✓							Class	Appl Sci	2021	-
MHCN [142]	Het, NU, MC	✓	✓	✓						Recom	TheWebConf	2021	Coder-Yu/QRec
HNN [105]	Hom, NU	✓	✓		✓					LP	TheWebConf	2021	-
DualHGNN [132]	Hom, NU, MC	✓	✓	✓						Class, LP	TheWebConf	2021	xuehansheng/DualHGNN
KHNN [71]	Hom, NU, MC	✓	✓							Recom	DASFAA	2021	-
SSF [46]	Hom, U	✓	✓	✓						LP	DASFAA	2021	-
STHAN-SR [97]	Hom, U, D	✓	✓	✓	✓					Regr	AAAI	2021	-
SHARE [119]	Hom, NU	✓, &	✓	✓	✓					Recom	SDM	2021	-
[101]	Hom, NU	✓, &	✓							LP	SDM	2021	-
MHGNN [1]	Hom, NU	✓	✓	✓						Class	TIP	2021	-
[130]	Het, NU, D	✓	✓	✓	✓					Regr	JIM	2021	-
HeteHG-VAE [31]	Het, NU	✓, &	✓	✓				✓		LP	PAMI	2021	haoyfan/HeteHG-VAE
UniGNN [52]	Hom, NU	✓, &	✓	✓						Class	IJCAI	2021	OneForward/UniGNN
[38]	Het, NU	✓	✓	✓	✓					LP	WWW	2021	-
S ² HGN [77]	Hom, NU, MC	✓	✓							Class	SPIE RS	2021	-
pLapHGNN* [76]	Het, NU	✓	✓				✓			Class	TMM	2021	-
DualHGNN [125]	Hom, NU, MC	✓	✓	✓						Class	J Kno Sys	2021	-
(Res Multi)HGNN [49]	Hom, NU	✓	✓	✓						Class	ICIP	2021	OneForward/ResMHGNN
HNN-HM [69]	Hom, U, Dir	✓	✓						✓	Class	ICCV	2021	-
H ² SeqRec [68]	Het, NU, MC, D	✓	✓							Recom	CIKM	2021	Abigale001/h2seqrec
HHGR [146]	Hom, NU	✓	✓	✓						Recom	CIKM	2021	0411tony/HHGR
HyperCTR [45]	Hom, NU, D	✓	✓							Recom	CIKM	2021	-
HybridHGNN [50]	Hom, NU, MC	✓	✓							Class	PRVC	2021	-
HGDD [85]	Het, NU	✓	✓							Class, LP	ISBRA	2021	-
HGNNa [27]	Hom, NU	✓	✓	✓						Recom	JPCS	2021	-
HGWNN [81]	Hom, NU	✓	✓				✓			Class	Neurocom.	2021	-
EHGNN [59]	Hom, NU	✓, &	✓	✓						Class	NeurIPS	2021	harryjo97/EHGNN
HOT [62]	Hom, U	✓	✓	✓	✓					LP	NeurIPS	2021	hw9730/hot
HyperTeNet [115]	Het, U, MC	✓	✓	✓						Recom	ICDM	2021	mvijaikumar/HyperTeNet
HyperGroup [42]	Hom, NU	✓	✓	✓						Recom	TOIS	2021	-
F ⁺ HNN [78]	Hom, NU, MC	✓	✓							Class	TGRS	2022	-
DHAT [75]	Hom, NU, Dir	✓	✓	✓						Regr	ITS	2022	-
[122]	Het, NU	✓	✓	✓		✓				Recom	WWW	2022	-
HyperINF [57]	Hom, NU, D, MC	✓	✓	✓						Recom	TUSC	2022	-
HEMR [66]	Het, NU, Dir	✓	✓					✓		Recom	TNNLS	2022	piciuslab/HEMR
GC-HGNN [88]	Hom, NU	✓	✓							Recom	J ECRA	2022	-
HRSC [151]	Het, NU	✓, &	✓					✓		Class, LP	Appl Sci	2022	-
IHGNN [18]	Het, U	✓, &	✓	✓						Recom	TheWebConf	2022	CDboyOne/IHGNN
AllSet [19]	Hom, NU	✓, &	✓	✓						Class	ICLR	2022	jianhao2016/AllSet
HyperSar [110]	Het, NU	✓, &	✓	✓						Recom	ECIR	2022	naver/hypersar
HT-HGNN [120]	Hom, NU, D, MC	✓	✓			✓				Regr	TITS	2022	-
[106]	Hom, NU, D	✓, &	✓	✓	✓					Class	TKDE	2022	-
HCCF [128]	Hom, NU	✓	✓	✓						Recom	SIGIR	2022	akaxlh/HCCF
HGNN* [37]	Hom, NU	✓	✓							Class, Recom	PAMI	2022	iMoonLab/DeepHypergraph
SHT [129]	Hom, NU	✓, &	✓	✓	✓					Recom	KDD	2022	akaxlh/SHT
DH-HGNN [43]	Hom, NU	✓	✓	✓	✓					Recom	SIGIR	2022	-
LE [136]	Hom, NU	✓	✓	✓						Class	CIKM	2022	ycq091044/LEGCN

Input HG: Hom/Het stands for homogeneous/heterogeneous, (N)U for (non-)uniform, MC for multi-channel, D for dynamic, and Dir for directed. Task: Class stands for classification, LP for link prediction, Regr for regression, and Recm for Recommendation. All methods can handle attributed nodes.

G DATASETS

Table 4 lists the datasets used by the works reviewed. For each dataset, we detail whether it belongs to a specific category, the link where it can be downloaded, a reference to the paper introducing it (if any), which methods have been tested on it and for which tasks, and how it has been modeled with a hypergraph.

Table 4. Most Commonly used Public Datasets by the Articles Reviewed

Dataset type	Dataset	Link (https://tinyurl.com/)	Class	Clus	LP	Recom	Regr	Other	Input setting	Used by
Bookmarks	Delicious.us [39]	delicious-db					✓		Het, NU	[150]
	CiteULike [39, 116]	citeulike-db					✓		Hom/Het, NU, MC	[54, 150]
Co-authorship / Co-citation	AMiner [109]	aminer-db	✓	✓					Het, NU	[22]
	ACM [123]	acm-data							Het, NU	[38]
	DBLP* [36, 139]	dblp-net dblp-bip aminer-dblp	✓	✓		✓			Hom/Het, NU, MC	[3, 19, 28, 31, 38, 40, 41, 47, 48, 52, 104, 105, 108, 125, 134, 135]
	Cora* [99]	cora-cit-network cora-coauth	✓	✓					Hom/Het, NU, MC	[2, 3, 19, 28, 35, 37, 50, 52, 56, 87, 90, 104, 105, 125, 134, 136]
	Citeseer [93]	citeseer	✓	✓					Hom, NU, MC	[2, 3, 19, 28, 35, 37, 50, 52, 56, 90, 125, 134, 136]
PubMed* [99]	pubmed-db pb-diabetes	✓	✓					Hom/Het, NU, MC	[2, 3, 19, 28, 33, 37, 50, 52, 87, 104, 134, 136]	
WebKB [24]	webkb-net	✓	✓					Hom, NU	[90]	
Categorical	20newsgroup [60]	20newsgroup	✓	✓					Hom, NU	[2, 19, 90, 94, 118, 136]
	Cancer [102]	cancer-db	✓	✓					Hom, NU	[72, 94]
	Chess [100]	chess-cat-db	✓	✓					Hom, NU	[94]
	Congress [98]	congress-votes	✓	✓					Hom, NU	[94]
	Covertype [9]	covertype	✓	✓					Hom, NU	[90]
	Letter [34]	letterrecog	✓	✓					Hom, NU	[90]
	Nursery [83]	nursery-db	✓	✓					Hom, NU	[94]
	Scene [12]	scenedb	✓	✓					Hom, NU, A	[103]
	Yeast [29]	yeastdataset	✓	✓					Hom, NU, A	[103]
	Zoo [34]	zoodb	✓	✓					Hom, NU	[19, 90, 94, 136, 149]
Purchase	Alibaba [132]	-	✓	✓					Hom/Het, (N)U, MC	[18, 132]
	Amazon* [67, 80, 139]	amazon-meta amznz-prod amznz-rev	✓	✓		✓			Hom/Het, (N)U, D, MC	[17, 18, 68, 90, 108, 118, 128, 132]
	Diginetica	diginetica	✓	✓					Hom/Het, (N)U	[18, 27, 88, 119, 131]
	Tmall	tmall-ijcai15	✓	✓					Hom/Het, NU	[88, 122, 129, 135]
	YooChoose [7]	yoochoose	✓	✓					Hom, U, D	[27, 119]
Biology / Chemistry	CMP	pmh-data-ch					✓		Het, NU, D	[130]
	CTD [143]	ctd-data	✓	✓					Het, NU	[85]
	Drug-Drug Interactions [5]	-				✓			Het, NU	[5]
	Drug-Target Interactions	dt-inter	✓	✓					Hom, NU, MC	[132]
	FAERS	drug-faers	✓	✓					Het, (N)U	[5, 51, 62, 112, 147, 151]
	IAF1260 [32]	iAF1260	✓	✓					Het, NU, D	[135]
	iJO1366 [84]	iJO1366-ecoli	✓	✓					Het, NU, D	[135]
	USPTO [58]	uspto-db	✓	✓					Het, NU, D	[135]
	GPS [148]	-	✓	✓					Hom/Het, (N)U	[51, 62, 112, 147, 151]
	Gowalla [20]	gowalla-db	✓	✓					Hom, NU	[129]
Images	AR	ar-database						✓	Hom, NU, A	[53]
	Botswana	botswana-img	✓	✓					Hom, NU, A, MC	[74, 78, 107, 144]
	FERET [89]	color-feret						✓	Hom, NU, A	[53]
	Houses	house-img	✓	✓					Hom, (N)U, Dir	[69, 91]
	Indian Pines [4]	indian-pines	✓	✓					Hom, NU, A, MC	[73, 77, 78, 107, 144]
	JAFFE [25]	jaffe-db	✓	✓				✓	Hom, NU, A	[53]
	KSC	ksc-db-img	✓	✓					Hom, NU, A, MC	[74, 77, 78]
	LFW-A [124]	lfw-db-img	✓	✓				✓	Hom, NU, A	[53]
	ModelNet40 [127]	modelnet40	✓	✓					Hom/Het, NU, MC	[1, 19, 33, 37, 49, 50, 76, 81, 136]
	MS-COCO [70]	mscoco-db	✓	✓					Hom, NU	[126]
	NUS-WIDE [23]	nus-wide-db	✓	✓					Het, NU	[21, 126]
	NTU [14]	http://3d.csie.ntu.edu.tw/	✓	✓					Hom/Het, NU, MC	[1, 19, 33, 37, 49, 50, 76, 81, 136]
	ORL [95]	faces-ori	✓	✓				✓	Hom, NU, A	[53]
	Pascal VOC [30]	pascal-voc-2007	✓	✓					Hom, (N)U, Dir	[69, 126]
	Pavia University	pavia-uni	✓	✓					Hom, NU, A, MC	[73, 78, 107]
Visual Genome [65]	visual-genome	✓	✓					Hom, NU	[126]	
Yale [6]	yale-faces-db-img	✓	✓				✓	Hom, NU, A	[53]	
Miscellanea	ReVerb45k [114]	reverb45k	✓	✓				Het, U, D	[135]	
Movies	CAMRa2011*	CAMRa2011		✓		✓			Hom/Het, NU	[55, 146]
	IMDB*	imdb-movie-db	✓	✓					Hom/Het, NU, MC	[31, 47, 48, 59, 125]
	LDOS-CoMoDa [82]	ldos-comoda				✓			Het, NU	[141]
	Micro-Video 1.7M [16]	micro-video	✓	✓					Hom, NU, D	[45]
	MovieLens* [44]	movie-lens	✓	✓					Hom/Het, (N)U, MC, D	[37, 45, 51, 54, 62, 71, 110, 112, 128, 147, 151]
Q&A	Yahoo* [61, 113]	yahoo-db	✓	✓					Hom, NU, A	[103]
Review	Goodreads* [117, 118]	goodreads-db	✓	✓		✓			Het, NU, D	[68, 115, 118]
	Movie review	movie-reviews-db	✓	✓					Het, NU	[118]
	Yelp*	yelp-db	✓	✓	✓	✓			Hom/Het, NU	[17, 19, 31, 38, 40-43, 105, 128, 129, 142]

(Continued)

Table 4. Continued

Dataset type	Dataset	Link (https://tinyurl.com/)	Class	Clus	LP	Recom	Regr	Other	Input setting	Used by
Social networks	Baidu (feed & news) [54]	-				✓			Hom, NU, MC	[54]
	Foursquare [137]	foursquare-net				✓			Het, U	[111, 137, 138]
	Douban	douban-db				✓	✓		Hom/Het, (N)U, MC	[31, 42, 43, 46, 142, 146]
	Douban-Weibo [15]	-				✓			Hom, NU	[15]
	Facebook-Twitter [15]	-				✓			Hom, NU	[15]
	Friendster [139]	friendster-net				✓			Hom, NU	[108]
	LiveJournal [139]	livejournal-net				✓			Hom, NU	[108]
	MaFengWo	-					✓		Het, NU	[55]
	Sina	-		✓					Hom, NU, D	[106]
	Twitter	-		✓					Hom, NU, D	[106]
	YouTube [139]	youtube-net-comm				✓			Hom, NU	[108]
	Weeplace [96]	weeplace-sn				✓	✓		Hom, NU	[146]
Weibo	-				✓	✓		Hom, (N)U, D, MC	[46, 57]	
Songs	#nowplaying [145]	nowplaying-db				✓			Hom, NU	[88, 131]
	Last.FM	last-fm-db				✓			Hom/Het, NU, MC	[71, 108, 110, 142]
	Spotify [8]	million-songs spotify-db				✓			Het, NU, Dir	[66, 115]
Text	Ohsumed Reuters	oh-r8-r52	✓						Het, NU	[118]
	wordnet [11, 79]	word-net	✓		✓				Het, (N)U	[51, 112, 147, 151]

Input setting: Hom/Het stands for homogeneous/heterogeneous, (N)U for (non-)uniform, MC for multi-channel, D for dynamic, and Dir for directed. The symbol * means that the specific dataset is available in multiple versions. †The NTU dataset is not reachable from our location. All links were accessed on the 12th of June, 2023.

REFERENCES

- [1] J. Bai, B. Gong, Y. Zhao, F. Lei, C. Yan, and Y. Gao. 2021. Multi-scale representation learning on hypergraph for 3D shape retrieval and recognition. *IEEE Transactions on Image Processing* 30 (2021), 5327–5338. <https://doi.org/10.1109/TIP.2021.3082765>
- [2] S. Bai, F. Zhang, and P. H. S. Torr. 2021. Hypergraph convolution and hypergraph attention. *Pattern Recognition* 110 (2021), 107637. <https://doi.org/10.1016/j.patcog.2020.107637>
- [3] S. Bandyopadhyay, K. Das, and M. N. Murty. 2020. Hypergraph attention isomorphism network by learning line graph expansion. In *Proceedings of the 2020 IEEE International Conference on Big Data (Big Data '20)*. 669–678. <https://doi.org/10.1109/BigData50022.2020.9378335>
- [4] M. F. Baumgardner, L. L. Biehl, and D. A. Landgrebe. 2015. 220 Band AVIRIS Hyperspectral Image Data Set: June 12, 1992 Indian Pine Test Site 3. <https://doi.org/doi:10.4231/R7RX991C>
- [5] I. M. Baytas, C. Xiao, F. Wang, A. K. Jain, and J. Zhou. 2018. Heterogeneous hyper-network embedding. In *Proceedings of the 2018 IEEE International Conference on Data Mining (ICDM'18)*. 875–880. <https://doi.org/10.1109/ICDM.2018.00104>
- [6] P. N. Belhumeur, J. P. Hespanha, and D. J. Kriegman. 1997. Eigenfaces vs. Fisherfaces: Recognition using class specific linear projection. *IEEE Transactions on Pattern Analysis and Machine Intelligence* 19, 7 (1997), 711–720. <https://doi.org/10.1109/34.598228>
- [7] D. Ben-Shimon, A. Tsikinovsky, M. Friedmann, B. Shapira, L. Rokach, and J. Hoerle. 2015. RecSys challenge 2015 and the YOOCHOOSE dataset. In *Proceedings of the 9th ACM Conference on Recommender Systems (RecSys'15)*. Association for Computing Machinery, New York, NY, 357–358. <https://doi.org/10.1145/2792838.2798723>
- [8] T. Bertin-Mahieux, D. P. W. Ellis, B. Whitman, and P. Lamere. 2011. The million song dataset. In *Proceedings of the 12th International Conference on Music Information Retrieval (ISMIR'11)*.
- [9] J. A. Blackard and D. J. Dean. 1999. Comparative accuracies of artificial neural networks and discriminant analysis in predicting forest cover types from cartographic variables. *Computers and Electronics in Agriculture* 24, 3 (1999), 131–151. [https://doi.org/10.1016/S0168-1699\(99\)00046-0](https://doi.org/10.1016/S0168-1699(99)00046-0)
- [10] M. Bolla. 1993. Spectra, Euclidean representations and clusterings of hypergraphs. *Discrete Mathematics* 117, 1–3 (1993), 19–39. [https://doi.org/10.1016/0012-365X\(93\)90322-K](https://doi.org/10.1016/0012-365X(93)90322-K)
- [11] A. Bordes, N. Usunier, A. Garcia-Duran, J. Weston, and O. Yakhnenko. 2013. Translating embeddings for modeling multi-relational data. In *Advances in Neural Information Processing Systems*, C. J. Burges, L. Bottou, M. Welling, Z. Ghahramani, and K. Q. Weinberger (Eds.), Vol. 26. Curran Associates, Inc.
- [12] M. R. Boutell, J. Luo, X. Shen, and C. M. Brown. 2004. Learning multi-label scene classification. *Pattern Recognition* 37, 9 (2004), 1757–1771. <https://doi.org/10.1016/j.patcog.2004.03.009>
- [13] C. Chen, Z. Cheng, Z. Li, and M. Wang. 2020. Hypergraph attention networks. In *Proceedings of the 2020 IEEE 19th International Conference on Trust, Security and Privacy in Computing and Communications (TrustCom'20)*. 1560–1565. <https://doi.org/10.1109/TrustCom50675.2020.00215>

- [14] D.-Y. Chen, X.-P. Tian, Y.-T. Shen, and M. Ouhyoung. 2003. On visual similarity based 3D model retrieval. *Computer Graphics Forum* 22, 3 (2003), 223–232. <https://doi.org/10.1111/1467-8659.00669>
- [15] H. Chen, H. Yin, X. Sun, T. Chen, G. Bogdan, and K. Musial. 2020. Multi-level graph convolutional networks for cross-platform anchor link prediction. In *Proceedings of the 26th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining (KDD'20)*. Association for Computing Machinery, New York, NY, 1503–1511. <https://doi.org/10.1145/3394486.3403201>
- [16] X. Chen, D. Liu, Z.-J. Zha, W. Zhou, Z. Xiong, and Y. Li. 2018. Temporal hierarchical attention at category- and item-level for micro-video click-through prediction. In *Proceedings of the 26th ACM International Conference on Multimedia (MM'18)*. Association for Computing Machinery, New York, NY, 1146–1153. <https://doi.org/10.1145/3240508.3240617>
- [17] X. Chen, K. Xiong, Y. Zhang, L. Xia, D. Yin, and J. X. Huang. 2020. Neural feature-aware recommendation with signed hypergraph convolutional network. *ACM Transactions on Information Systems* 39, 1 (2020), Article 8, 22 pages. <https://doi.org/10.1145/3423322>
- [18] D. Cheng, J. Chen, W. Peng, W. Ye, F. Lv, T. Zhuang, X. Zeng, and X. He. 2022. IHGNN: Interactive hypergraph neural network for personalized product search. In *Proceedings of the ACM Web Conference 2022 (WWW'22)*. Association for Computing Machinery, New York, NY, 256–265. <https://doi.org/10.1145/3485447.3511954>
- [19] E. Chien, C. Pan, J. Peng, and O. Milenkovic. 2022. You are AllSet: A multiset function framework for hypergraph neural networks. In *Proceedings of the International Conference on Learning Representations (ICLR'22)*.
- [20] Eunjoon Cho, Seth A. Myers, and Jure Leskovec. 2011. Friendship and mobility: User movement in location-based social networks. In *Proceedings of the 17th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining (KDD'11)*. Association for Computing Machinery, New York, NY, 1082–1090. <https://doi.org/10.1145/2020408.2020579>
- [21] Y. Chu, C. Feng, and C. Guo. 2018. Social-guided representation learning for images via deep heterogeneous hypergraph embedding. In *Proceedings of the 2018 IEEE International Conference on Multimedia and Expo (ICME'18)*. 1–6. <https://doi.org/10.1109/ICME.2018.8486506>
- [22] Y. Chu, C. Feng, C. Guo, Y. Wang, and J. N. Hwang. 2019. Event2vec: Heterogeneous hypergraph embedding for event data. *IEEE International Conference on Data Mining Workshops (ICDMW'19)*, 1022–1029. <https://doi.org/10.1109/ICDMW.2018.00147>
- [23] T.-S. Chua, J. Tang, R. Hong, H. Li, Z. Luo, and Y. Zheng. 2009. NUS-WIDE: A real-world web image database from national university of Singapore. In *Proceedings of the ACM International Conference on Image and Video Retrieval (CIVR'09)*. Association for Computing Machinery, New York, NY, Article 48, 9 pages. <https://doi.org/10.1145/1646396.1646452>
- [24] M. Craven, D. DiPasquo, D. Freitag, A. McCallum, T. Mitchell, K. Nigam, and S. Slattery. 1998. Learning to extract symbolic knowledge from the World Wide Web. In *Proceedings of the 15th National/10th Conference on Artificial Intelligence/Innovative Applications of Artificial Intelligence (AAAI'98/IAAI'98)*. American Association for Artificial Intelligence, 509–516.
- [25] M. N. Dailey, C. Joyce, M. J. Lyons, M. Kamachi, H. Ishi, J. Gyoba, and G. W. Cottrell. 2010. Evidence and a computational explanation of cultural differences in facial expression recognition. *Emotion* 10, 6 (2010), 874–893.
- [26] K. Ding, J. Wang, J. Li, D. Li, and H. Liu. 2020. Be more with less: Hypergraph attention networks for inductive text classification. In *Proceedings of the 2020 Conference on Empirical Methods in Natural Language Processing (EMNLP'20)*. Association for Computational Linguistics, 4927–4936. <https://doi.org/10.18653/v1/2020.emnlp-main.399>
- [27] M. Ding, X. Lin, B. Zeng, and Y. Chai. 2021. Hypergraph neural networks with attention mechanism for session-based recommendation. *Journal of Physics: Conference Series* 2082, 1 (2021), 012007. <https://doi.org/10.1088/1742-6596/2082/1/012007>
- [28] Y. Dong, W. Sawin, and Y. Bengio. 2020. HNNH: Hypergraph networks with hyperedge neurons. In *Graph Representation Learning and Beyond Workshop at ICML 2020*.
- [29] A. Elisseeff and J. Weston. 2001. A kernel method for multi-labelled classification. In *Advances in Neural Information Processing Systems*, T. Dietterich, S. Becker, and Z. Ghahramani (Eds.), Vol. 14. MIT Press.
- [30] M. Everingham, Van Gool, C. K. I. Williams, J. Winn, and A. Zisserman. 2010. The Pascal visual object classes (VOC) challenge. *International Journal of Computer Vision* 88, 2 (2010), 303–338. <https://doi.org/10.1007/s11263-009-0275-4>
- [31] H. Fan, F. Zhang, Y. Wei, Z. Li, C. Zou, Y. Gao, and Q. Dai. 2021. Heterogeneous hypergraph variational autoencoder for link prediction. *IEEE Transactions on Pattern Analysis and Machine Intelligence* 44, 8 (2021), 4125–4138. <https://doi.org/10.1109/TPAMI.2021.3059313>
- [32] A. M. Feist, C. S. Henry, J. L. Reed, M. Krummenacker, A. R. Joyce, P. D. Karp, L. J. Broadbelt, V. Hatzimanikatis, and B. Ø. Palsson. 2007. A genome-scale metabolic reconstruction for *Escherichia coli* K-12 MG1655 that accounts for 1260 ORFs and thermodynamic information. *Molecular Systems Biology* 3 (2007), 121.
- [33] Y. Feng, H. You, Z. Zhang, R. Ji, and Y. Gao. 2019. Hypergraph neural networks. *Proceedings of the AAAI Conference on Artificial Intelligence* 33, 1 (2019), 3558–3565. <https://doi.org/10.1609/aaai.v33i01.33013558>

- [34] P. W. Frey and D. J. Slate. 1991. Letter recognition using Holland-style adaptive classifiers. *Machine Learning* 6, 2 (1991), 161–182. <https://doi.org/10.1007/BF00114162>
- [35] S. Fu, W. Liu, Y. Zhou, and L. Nie. 2019. HpLapGCN: Hypergraph p -Laplacian graph convolutional networks. *Neurocomputing* 362 (2019), 166–174. <https://doi.org/10.1016/j.neucom.2019.06.068>
- [36] M. Gao, L. Chen, X. He, and A. Zhou. 2018. BiNE: Bipartite network embedding. In *Proceedings of the 41st International ACM SIGIR Conference on Research & Development in Information Retrieval (SIGIR'18)*. Association for Computing Machinery, New York, NY, 715–724. <https://doi.org/10.1145/3209978.3209987>
- [37] Y. Gao, Y. Feng, S. Ji, and R. Ji. 2023. HGNN+: General hypergraph neural networks. *IEEE Transactions on Pattern Analysis and Machine Intelligence* 45, 3 (2023), 3181–3199. <https://doi.org/10.1109/TPAMI.2022.3182052>
- [38] Y. Guan, X. Sun, and Y. Sun. 2021. Sparse relation prediction based on hypergraph neural networks in online social networks. *World Wide Web* 26, 1 (2021), 7–31. <https://doi.org/10.1007/s11280-021-00936-w>
- [39] Z. Guan, C. Wang, J. Bu, C. Chen, K. Yang, D. Cai, and X. He. 2010. Document recommendation in social tagging services. In *Proceedings of the 19th International Conference on World Wide Web (WWW'10)*. Association for Computing Machinery, New York, NY, 391–400. <https://doi.org/10.1145/1772690.1772731>
- [40] H. Gui, J. Liu, F. Tao, M. Jiang, B. Norick, and J. Han. 2016. Large-scale embedding learning in heterogeneous event data. In *Proceedings of the 2016 IEEE 16th International Conference on Data Mining (ICDM'16)*, 907–912. <https://doi.org/10.1109/icdm.2016.0111>
- [41] H. Gui, J. Liu, F. Tao, M. Jiang, B. Norick, L. Kaplan, and J. Han. 2017. Embedding learning with events in heterogeneous information networks. *IEEE Transactions on Knowledge and Data Engineering* 29, 11 (2017), 2428–2441. <https://doi.org/10.1109/tkde.2017.2733530>
- [42] L. Guo, H. Yin, T. Chen, X. Zhang, and K. Zheng. 2021. Hierarchical hyperedge embedding-based representation learning for group recommendation. *ACM Transactions on Information Systems* 40, 1 (2021), Article 3, 27 pages. <https://doi.org/10.1145/3457949>
- [43] J. Han, Q. Tao, Y. Tang, and Y. Xia. 2022. DH-HGCN: Dual homogeneity hypergraph convolutional network for multiple social recommendations. In *Proceedings of the 45th International ACM SIGIR Conference on Research and Development in Information Retrieval (SIGIR'22)*. Association for Computing Machinery, New York, NY, 2190–2194. <https://doi.org/10.1145/3477495.3531828>
- [44] F. M. Harper and J. A. Konstan. 2015. The MovieLens datasets: History and context. *ACM Transactions on Interactive Intelligent Systems* 5, 4 (2015), Article 19, 19 pages. <https://doi.org/10.1145/2827872>
- [45] L. He, H. Chen, D. Wang, S. Jameel, P. Yu, and G. Xu. 2021. Click-through rate prediction with multi-modal hypergraphs. In *Proceedings of the 30th ACM International Conference on Information & Knowledge Management (CIKM'21)*. Association for Computing Machinery, New York, NY, 690–699. <https://doi.org/10.1145/3459637.3482327>
- [46] Z. Hu, J. Wang, S. Chen, and X. Du. 2021. A semi-supervised framework with efficient feature extraction and network alignment for user identity linkage. In *Proceedings of the 26th International Conference of Database Systems for Advanced Applications (DASFAA'21)*. Springer-Verlag, Berlin, 675–691. https://doi.org/10.1007/978-3-030-73197-7_46
- [47] J. Huang, Ch. Chen, F. Ye, W. Hu, and Z. Zheng. 2020. Nonuniform hyper-network embedding with dual mechanism. *ACM Transactions on Information Systems* 38, 3, Article 28 (2020). <https://doi.org/10.1145/3388924>
- [48] J. Huang, C. Chen, F. Ye, J. Wu, Z. Zheng, and G. Ling. 2019. Hyper2vec: Biased random walk for hyper-network embedding. *Database Systems for Advanced Applications, Lecture Notes in Computer Science*, Vol. 11448. Springer International Publishing, Cham, 273–277. https://doi.org/10.1007/978-3-030-18590-9_27
- [49] J. Huang, X. Huang, and J. Yang. 2021. Residual enhanced multi-hypergraph neural network. In *2021 IEEE International Conference on Image Processing (ICIP'21)*. 3657–3661. <https://doi.org/10.1109/ICIP42928.2021.9506153>
- [50] J. Huang, F. Lei, S. Wang, S. Wang, and Q. Dai. 2021. Hypergraph convolutional network with hybrid higher-order neighbors. *Pattern Recognition and Computer Vision*. Springer International Publishing, Cham, 103–114. https://doi.org/10.1007/978-3-030-88013-2_9
- [51] J. Huang, X. Liu, and Y. Song. 2019. Hyper-path-based representation learning for hyper-networks. In *Proceedings of the 28th ACM International Conference on Information and Knowledge Management (CIKM'19)*. Association for Computing Machinery, New York, NY, 449–458. <https://doi.org/10.1145/3357384.3357871>
- [52] J. Huang and J. Yang. 2021. UniGNN: A unified framework for graph and hypergraph neural networks. In *Proceedings of the 30th International Joint Conference on Artificial Intelligence (IJCAI'21)*. International Joint Conferences on Artificial Intelligence Organization, 2563–2569. <https://doi.org/10.24963/ijcai.2021/353>
- [53] S. Huang, D. Yang, Y. Ge, and X. Zhang. 2016. Discriminant hyper-Laplacian projections and its scalable extension for dimensionality reduction. *Neurocomputing* 173 (2016), 145–153. <https://doi.org/10.1016/j.neucom.2015.01.101>
- [54] S. Ji, Y. Feng, R. Ji, X. Zhao, W. Tang, and Y. Gao. 2020. Dual channel hypergraph collaborative filtering. In *Proceedings of the International Conference on Knowledge Discovery & Data Mining (KDD'20)*. Association for Computing Machinery, New York, NY, 2020–2029. <https://doi.org/10.1145/3394486.3403253>

- [55] R. Jia, X. Zhou, L. Dong, and S. Pan. 2021. Hypergraph convolutional network for group recommendation. In *Proceedings of the 2021 IEEE International Conference on Data Mining (ICDM'21)*. 260–269. <https://doi.org/10.1109/ICDM51629.2021.00036>
- [56] J. Jiang, Y. Wei, Y. Feng, J. Cao, and Y. Gao. 2019. Dynamic hypergraph neural networks. In *Proceedings of the 28th International Joint Conference on Artificial Intelligence (IJCAI'19)*. International Joint Conferences on Artificial Intelligence Organization, 2635–2641. <https://doi.org/10.24963/ijcai.2019/366>
- [57] H. Jin, Y. Wu, H. Huang, Y. Song, H. Wei, and X. Shi. 2022. Modeling information diffusion with sequential interactive hypergraphs. *IEEE Transactions on Sustainable Computing* 7, 3 (2022), 644–655. <https://doi.org/10.1109/TSUSC.2022.3152366>
- [58] W. Jin, C. Coley, R. Barzilay, and T. Jaakkola. 2017. Predicting organic reaction outcomes with Weisfeiler-Lehman network. In *Advances in Neural Information Processing Systems*, I. Guyon, U. Von Luxburg, S. Bengio, H. Wallach, R. Fergus, S. Vishwanathan, and R. Garnett (Eds.), Vol. 30. Curran Associates, Inc.
- [59] J. Jo, J. Baek, S. Lee, D. Kim, M. Kang, and S. J. Hwang. 2021. Edge representation learning with hypergraphs. *Advances in Neural Information Processing Systems*, Vol. 34. Curran Associates, Inc., 7534–7546.
- [60] T. Joachims. 1997. A probabilistic analysis of the Rocchio algorithm with TFIDF for text categorization. In *Proceedings of the 14th International Conference on Machine Learning (ICML'97)*. Morgan Kaufmann Publishers Inc., San Francisco, CA, 143–151.
- [61] H. Kazawa, T. Izumitani, H. Taira, and E. Maeda. 2004. Maximal margin labeling for multi-topic text categorization. In *Advances in Neural Information Processing Systems*, L. Saul, Y. Weiss, and L. Bottou (Eds.), Vol. 17. MIT Press.
- [62] J. Kim, S. Oh, and S. Hong. 2021. Transformers generalize deepsets and can be extended to graphs and hypergraphs. In *Advances in Neural Information Processing Systems*, Vol. 34. Curran Associates, Inc., 28016–28028.
- [63] T. N. Kipf and M. Welling. 2017. Semi-supervised classification with graph convolutional networks. In *Proceedings of the International Conference on Learning Representations*.
- [64] E. B. Kosmatopoulos, M. M. Polycarpou, M. A. Christodoulou, and P. A. Ioannou. 1995. High-order neural network structures for identification of dynamical systems. *IEEE Transactions on Neural Networks* 6, 2 (1995), 422–431. <https://doi.org/10.1109/72.363477>
- [65] R. Krishna, Y. Zhu, O. Groth, J. Johnson, K. Hata, J. Kravitz, S. Chen, Y. Kalantidis, L.-J. Li, D. A. Shamma, M. S. Bernstein, and L. Fei-Fei. 2017. Visual genome: Connecting language and vision using crowdsourced dense image annotations. *International Journal of Computer Vision* 123, 1 (2017), 32–73. <https://doi.org/10.1007/s11263-016-0981-7>
- [66] V. La Gatta, V. Moscato, M. Pennone, M. Postiglione, and G. Sperli. 2022. Music recommendation via hypergraph embedding. *IEEE Transactions on Neural Networks and Learning Systems* (2022), 1–13. <https://doi.org/10.1109/TNNLS.2022.3146968>
- [67] J. Leskovec, L. A. Adamic, and B. A. Huberman. 2007. The dynamics of viral marketing. *ACM Transactions on Web* 1, 1 (2007), 5–es. <https://doi.org/10.1145/1232722.1232727>
- [68] Y. Li, H. Chen, X. Sun, Z. Sun, L. Li, L. Cui, P. S. Yu, and G. Xu. 2021. Hyperbolic hypergraphs for sequential recommendation. In *Proceedings of the 30th ACM International Conference on Information & Knowledge Management (CIKM'21)*. Association for Computing Machinery, New York, NY, 988–997. <https://doi.org/10.1145/3459637.3482351>
- [69] X. Liao, Y. Xu, and H. Ling. 2021. Hypergraph neural networks for hypergraph matching. In *Proceedings of the 2021 IEEE/CVF International Conference on Computer Vision (ICCV'21)*. 1246–1255. <https://doi.org/10.1109/ICCV48922.2021.00130>
- [70] T.-Y. Lin, M. Maire, S. Belongie, J. Hays, P. Perona, D. Ramanan, P. Dollár, and C. L. Zitnick. 2014. Microsoft COCO: Common objects in context. In *Computer Vision – ECCV 2014*. Springer International Publishing, Cham, 740–755.
- [71] B. Liu, P. Zhao, F. Zhuang, X. Xian, Y. Liu, and V. S. Sheng. 2021. Knowledge-aware hypergraph neural network for recommender systems. *Database Systems for Advanced Applications*. Springer International Publishing, Cham, 132–147. https://doi.org/10.1007/978-3-030-73200-4_9
- [72] Z. Liu, Z. Zhang, Y. Cai, Y. Miao, and Z. Chen. 2021. Semi-supervised classification via hypergraph convolutional extreme learning machine. *Applied Sciences* 11, 9 (2021), 3867. <https://doi.org/10.3390/app11093867>
- [73] F. Luo, B. Du, L. Zhang, L. Zhang, and D. Tao. 2019. Feature learning using spatial-spectral hypergraph discriminant analysis for hyperspectral image. *IEEE Transactions on Cybernetics* 49, 7 (2019), 2406–2419. <https://doi.org/10.1109/TCYB.2018.2810806>
- [74] F. Luo, G. Guo, Z. Lin, J. Ren, and X. Zhou. 2020. Semisupervised hypergraph discriminant learning for dimensionality reduction of hyperspectral image. *IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing* 13 (2020), 4242–4256. <https://doi.org/10.1109/JSTARS.2020.3011431>
- [75] X. Luo, J. Peng, and J. Liang. 2022. Directed hypergraph attention network for traffic forecasting. *IET Intelligent Transport Systems* 16, 1 (2022), 85–98. <https://doi.org/10.1049/itr2.12130>
- [76] X. Ma, W. Liu, Q. Tian, and Y. Gao. 2022. Learning representation on optimized high-order manifold for visual classification. *IEEE Transactions on Multimedia* 24 (2022), 3989–4001. <https://doi.org/10.1109/TMM.2021.3111500>

- [77] Z. Ma, Z. Jiang, and H. Zhang. 2021. Hyperspectral image classification using spectral-spatial hypergraph convolution neural network. In *Image and Signal Processing for Remote Sensing XXVII*, Vol. 11862. SPIE, 118620I. <https://doi.org/10.1117/12.2599787>
- [78] Z. Ma, Z. Jiang, and H. Zhang. 2022. Hyperspectral image classification using feature fusion hypergraph convolution neural network. *IEEE Transactions on Geoscience and Remote Sensing* 60 (2022), 1–14. <https://doi.org/10.1109/TGRS.2021.3123423>
- [79] George A. Miller. 1994. WordNet: A lexical database for English. In *Human Language Technology: Proceedings of a Workshop held at Plainsboro, New Jersey, March 8–11, 1994*. <https://aclanthology.org/H94-1111>.
- [80] J. Ni, J. Li, and J. McAuley. 2019. Justifying recommendations using distantly-labeled reviews and fine-grained aspects. In *Proceedings of the 2019 Conference on Empirical Methods in Natural Language Processing and the 9th International Joint Conference on Natural Language Processing (EMNLP-IJCNLP'19)*. Association for Computational Linguistics, 188–197. <https://doi.org/10.18653/v1/D19-1018>
- [81] L. Nong, J. Wang, J. Lin, H. Qiu, L. Zheng, and W. Zhang. 2021. Hypergraph wavelet neural networks for 3D object classification. *Neurocomputing* 463, C (2021), 580–595. <https://doi.org/10.1016/j.neucom.2021.08.006>
- [82] A. Odić, M. Tkalčić, J. F. Tasić, and A. Košir. 2013. Predicting and detecting the relevant contextual information in a movie-recommender system. *Interacting with Computers* 25, 1 (2013), 74–90. <https://doi.org/10.1093/iwc/iws003>
- [83] M. Olave, V. Rajkovic, and M. Bohanec. 1989. An application for admission in public school systems. *Expert Systems in Public Administration* 19, 7 (1989), 145–160.
- [84] J. D. Orth, T. M. Conrad, J. Na, J. A. Lerman, H. Nam, A. M. Feist, and B. Ø. Palsson. 2011. A comprehensive genome-scale reconstruction of *Escherichia coli* metabolism—2011. *Molecular Systems Biology* 7 (2011), 535.
- [85] S. Pang, K. Zhang, S. Wang, Y. Zhang, S. He, W. Wu, and S. Qiao. 2021. HGDD: A drug-disease high-order association information extraction method for drug repurposing via hypergraph. In *Proceedings of the 17th International Symposium on Bioinformatics Research and Applications (ISBRA'21)*. Springer-Verlag, Berlin, 424–435. https://doi.org/10.1007/978-3-030-91415-8_36
- [86] R. M. Pattanayak and H. S. Behera. 2018. Higher order neural network and its applications: A comprehensive survey. *Progress in Computing, Analytics and Networking*. Springer Singapore, Singapore, 695–709. https://doi.org/10.1007/978-981-10-7871-2_67
- [87] J. Payne. 2019. Deep hyperedges: A framework for transductive and inductive learning on hypergraphs. In *Proceedings of Neural Information Processing Systems*.
- [88] D. Peng and S. Zhang. 2022. GC-HGNN: A global-context supported hypergraph neural network for enhancing session-based recommendation. *Electronic Commerce Research and Applications* 52 (2022), 101129. <https://doi.org/10.1016/j.elerap.2022.101129>
- [89] P. J. Phillips, H. Wechsler, J. Huang, and P. J. Rauss. 1998. The FERET database and evaluation procedure for face-recognition algorithms. *Image and Vision Computing* 16, 5 (1998), 295–306. [https://doi.org/10.1016/S0262-8856\(97\)00070-X](https://doi.org/10.1016/S0262-8856(97)00070-X)
- [90] L. Pu and B. Faltings. 2012. Hypergraph learning with hyperedge expansion. In *Machine Learning and Knowledge Discovery in Databases*. Springer, Berlin, 410–425. https://doi.org/10.1007/978-3-642-33460-3_32
- [91] P. Ren, R. C. Wilson, and E. R. Hancock. 2008. Spectral embedding of feature hypergraphs. In *Structural, Syntactic, and Statistical Pattern Recognition*. 308–317. https://doi.org/10.1007/978-3-540-89689-0_35
- [92] J. A. Rodriguez. 2002. On the Laplacian eigenvalues and metric parameters of hypergraphs. *Linear and Multilinear Algebra* 50, 1 (2002), 1–14. <https://doi.org/10.1080/03081080290011692>
- [93] R. Rossi and N. Ahmed. 2015. The network data repository with interactive graph analytics and visualization. In *AAAI Conference on Artificial Intelligence*, Vol. 29. AAAI, New York, NY, 4292–4293.
- [94] S. Saito, D. P. Mandic, and H. Suzuki. 2018. Hypergraph p -Laplacian: A differential geometry view. *Proceedings of the AAAI Conference on Artificial Intelligence* 32, 1 (2018). <https://doi.org/10.1609/aaai.v32i1.11823>
- [95] F. S. Samaria and A. C. Harter. 1994. Parameterisation of a stochastic model for human face identification. In *Proceedings of the 1994 IEEE Workshop on Applications of Computer Vision*. 138–142. <https://doi.org/10.1109/ACV.1994.341300>
- [96] A. Sankar, Y. Wu, Y. Wu, W. Zhang, H. Yang, and H. Sundaram. 2020. GroupIM: A mutual information maximization framework for neural group recommendation. In *Proceedings of the 43rd International ACM SIGIR Conference on Research and Development in Information Retrieval (SIGIR'20)*. Association for Computing Machinery, New York, NY, 1279–1288. <https://doi.org/10.1145/3397271.3401116>
- [97] R. Sawhney, S. Agarwal, A. Wadhwa, T. Derr, and R. R. Shah. 2021. Stock selection via spatiotemporal hypergraph attention network: A learning to rank approach. *Proceedings of the AAAI Conference on Artificial Intelligence* 35, 1 (2021), 497–504. <https://doi.org/10.1609/aaai.v35i1.16127>
- [98] J. C. Schlimmer. 1987. *Concept Acquisition through Representational Adjustment*. Ph. D. Dissertation. Department of Information and Computer Science, University of California. <https://doi.org/10.5555/913421>
- [99] P. Sen, G. Namata, M. Bilgic, L. Getoor, B. Galligher, and T. Eliassi-Rad. 2008. Collective classification in network data. *AI Magazine* 29, 3 (2008), 93. <https://doi.org/10.1609/aimag.v29i3.2157>

- [100] A. D. Shapiro. 1987. *Structured Induction in Expert Systems*. Addison-Wesley Longman Publishing Co., Inc.. <https://doi.org/10.5555/32231>
- [101] B. Srinivasan, D. Zheng, and G. Karypis. 2021. Learning over families of sets—Hypergraph representation learning for higher order tasks. In *Proceedings of the 2021 SIAM International Conference on Data Mining (SDM'21)*. Siam Society, 756–764. <https://doi.org/10.1137/1.9781611976700.85>
- [102] W. N. Street, W. H. Wolberg, and O. L. Mangasarian. 1993. Nuclear feature extraction for breast tumor diagnosis. In *Biomedical Image Processing and Biomedical Visualization*, Raj S. Acharya and Dmitry B. Goldgof (Eds.), Vol. 1905. International Society for Optics and Photonics, SPIE, 861–870. <https://doi.org/10.1117/12.148698>
- [103] L. Sun, S. Ji, and J. Ye. 2008. Hypergraph spectral learning for multi-label classification. In *Proceedings of the International Conference on Knowledge Discovery and Data Mining (KDD'08)*. Association for Computing Machinery, New York, NY, 668–676. <https://doi.org/10.1145/1401890.1401971>
- [104] X. Sun, H. Yin, B. Liu, H. Chen, J. Cao, Y. Shao, and N. Q. Viet Hung. 2021. Heterogeneous hypergraph embedding for graph classification. In *Proceedings of the International Conference on Web Search and Data Mining (WSDM'21)*. Association for Computing Machinery, New York, NY, 725–733. <https://doi.org/10.1145/3437963.3441835>
- [105] X. Sun, H. Yin, B. Liu, H. Chen, Q. Meng, W. Han, and J. Cao. 2021. Multi-level hyperedge distillation for social linking prediction on sparsely observed networks. In *Proceedings of the Web Conference 2021 (WWW'21)*. Association for Computing Machinery, New York, NY, 2934–2945. <https://doi.org/10.1145/3442381.3449912>
- [106] X. Sun, H. Yin, B. Liu, Q. Meng, J. Cao, A. Zhou, and H. Chen. 2022. Structure learning via meta-hyperedge for dynamic rumor detection. *IEEE Transactions on Knowledge and Data Engineering* (2022), 1–12. <https://doi.org/10.1109/TKDE.2022.3221438>
- [107] Y. Sun, Sujuan Wang, Qingshan Liu, Renlong Hang, and Guangcan Liu. 2017. Hypergraph embedding for spatial-spectral joint feature extraction in hyperspectral images. *Remote Sensing* 9, 5 (2017). <https://doi.org/10.3390/rs9050506>
- [108] J. Sybrandt and I. Safro. 2019. FOBE and HOBE: First- and High-Order Bipartite Embeddings. <https://arxiv.org/abs/1905.10953>
- [109] J. Tang, J. Zhang, L. Yao, J. Li, L. Zhang, and Z. Su. 2008. ArnetMiner: Extraction and mining of academic social networks. In *Proceedings of the 14th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining (KDD'08)*. Association for Computing Machinery, New York, NY, 990–998. <https://doi.org/10.1145/1401890.1402008>
- [110] T. Thonet, J.-M. Renders, M. Choi, and J. Kim. 2022. Joint personalized search and recommendation with hypergraph convolutional networks. In *Advances in Information Retrieval (ECIR'22)*. Springer-Verlag, Berlin, 443–456. https://doi.org/10.1007/978-3-030-99736-6_30
- [111] H. T. Trung, T. Van Vinh, N. T. Tam, J. Jo, H. Yin, and N. Q. V. Hung. 2022. Learning holistic interactions in LBSNs with high-order, dynamic, and multi-role contexts. *IEEE Transactions on Knowledge and Data Engineering* 35, 5 (2022), 5002–5016. <https://doi.org/10.1109/TKDE.2022.3150792>
- [112] K. Tu, P. Cui, X. Wang, F. Wang, and W. Zhu. 2018. Structural deep embedding for hyper-networks. In *Proceedings of the 32nd AAAI Conference on Artificial Intelligence (AAAI'18)*. AAAI Press, Article 53. <https://doi.org/10.5555/3504035.3504088>
- [113] N. Ueda and K. Saito. 2002. Parametric mixture models for multi-labeled text. In *Advances in Neural Information Processing Systems*, S. Becker, S. Thrun, and K. Obermayer (Eds.), Vol. 15. MIT Press.
- [114] S. Vashishth, P. Jain, and P. Talukdar. 2018. CESI: Canonicalizing open knowledge bases using embeddings and side information. In *Proceedings of the 2018 World Wide Web Conference (WWW'18)*. International World Wide Web Conferences Steering Committee, 1317–1327. <https://doi.org/10.1145/3178876.3186030>
- [115] M. Vijaikumar, D. Hada, and S. Shevade. 2021. HyperTeNet: Hypergraph and transformer-based neural network for personalized list continuation. In *2021 IEEE International Conference on Data Mining (ICDM'21)*. 1210–1215. <https://doi.org/10.1109/ICDM51629.2021.00146>
- [116] H. Wang, B. Chen, and W.-J. Li. 2013. Collaborative topic regression with social regularization for tag recommendation. In *Proceedings of the 23rd International Joint Conference on Artificial Intelligence (IJCAI'13)*. AAAI Press, 2719–2725. <https://doi.org/10.5555/2540128.2540520>
- [117] J. Wang and J. Caverlee. 2019. Recurrent recommendation with local coherence. In *Proceedings of the 12th ACM International Conference on Web Search and Data Mining (WSDM'19)*. Association for Computing Machinery, New York, NY, 564–572. <https://doi.org/10.1145/3289600.3291024>
- [118] J. Wang, K. Ding, L. Hong, H. Liu, and J. Caverlee. 2020. Next-item recommendation with sequential hypergraphs. In *Proceedings of the 43rd International ACM SIGIR Conference on Research and Development in Information Retrieval (SIGIR'20)*. ACM, New York, NY, 1101–1110. <https://doi.org/10.1145/3397271.3401133>
- [119] J. Wang, K. Ding, Z. Zhu, and J. Caverlee. 2021. Session-based recommendation with hypergraph attention networks. In *Proceedings of the SIAM International Conference on Data Mining*. Society for Industrial and Applied Mathematics, 82–90. <https://doi.org/10.1137/1.9781611976700.10>

- [120] J. Wang, Y. Zhang, L. Wang, Y. Hu, X. Piao, and B. Yin. 2022. Multitask hypergraph convolutional networks: A heterogeneous traffic prediction framework. *IEEE Transactions on Intelligent Transportation Systems* (2022), 1–11. <https://doi.org/10.1109/TITS.2022.3168879>
- [121] J. Wang, Y. Zhang, Y. Wei, Y. Hu, X. Piao, and B. Yin. 2021. Metro passenger flow prediction via dynamic hypergraph convolution networks. *IEEE Transactions on Intelligent Transportation Systems* 22, 12 (2021), 7891–7903. <https://doi.org/10.1109/TITS.2021.3072743>
- [122] N. Wang, S. Wang, Y. Wang, Q. Z. Sheng, and M. A. Orgun. 2022. Exploiting intra- and inter-session dependencies for session-based recommendations. *World Wide Web* 25, 1 (2022), 425–443. <https://doi.org/10.1007/s11280-021-00930-2>
- [123] Xiao Wang, Houye Ji, Chuan Shi, Bai Wang, Yanfang Ye, Peng Cui, and Philip S. Yu. 2019. Heterogeneous graph attention network. In *The World Wide Web Conference (WWW'19)*. Association for Computing Machinery, New York, NY, 2022–2032. <https://doi.org/10.1145/3308558.3313562>
- [124] L. Wolf, T. Hassner, and Y. Taigman. 2010. Similarity scores based on background samples. In *Computer Vision—ACCV 2009*, H. Zha, R. Taniguchi, and S. Maybank (Eds.). Springer, Berlin, 88–97. https://doi.org/10.1007/978-3-642-12304-7_9
- [125] L. Wu, D. Wang, K. Song, S. Feng, Y. Zhang, and G. Yu. 2021. Dual-view hypergraph neural networks for attributed graph learning. *Knowledge-Based Systems* 227 (2021), 107185. <https://doi.org/10.1016/j.knsys.2021.107185>
- [126] X. Wu, Q. Chen, W. Li, Y. Xiao, and B. Hu. 2020. AdaHGNN: Adaptive hypergraph neural networks for multi-label image classification. In *Proceedings of the International Conference on Multimedia (MM'20)*. ACM, New York, NY, 284–293. <https://doi.org/10.1145/3394171.3414046>
- [127] Z. Wu, S. Song, A. Khosla, F. Yu, L. Zhang, X. Tang, and J. Xiao. 2015. 3D ShapeNets: A deep representation for volumetric shapes. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition (CVPR'15)*.
- [128] L. Xia, C. Huang, Y. Xu, J. Zhao, D. Yin, and J. Huang. 2022. Hypergraph contrastive collaborative filtering. In *Proceedings of the 45th International ACM SIGIR Conference on Research and Development in Information Retrieval (SIGIR'22)*. Association for Computing Machinery, New York, NY, 70–79. <https://doi.org/10.1145/3477495.3532058>
- [129] L. Xia, C. Huang, and C. Zhang. 2022. Self-supervised hypergraph transformer for recommender systems. In *Proceedings of the 28th ACM SIGKDD Conference on Knowledge Discovery and Data Mining (KDD'22)*. Association for Computing Machinery, New York, NY, 2100–2109. <https://doi.org/10.1145/3534678.3539473>
- [130] L. Xia, P. Zheng, X. Huang, and C. Liu. 2021. A novel hypergraph convolution network-based approach for predicting the material removal rate in chemical mechanical planarization. *Journal of Intelligent Manufacturing* 33, 8 (2021), 2295–2306. <https://doi.org/10.1007/s10845-021-01784-1>
- [131] X. Xia, H. Yin, J. Yu, Q. Wang, L. Cui, and X. Zhang. 2021. Self-supervised hypergraph convolutional networks for session-based recommendation. *Proceedings of the AAAI Conference on Artificial Intelligence* 35, 5 (2021), 4503–4511. <https://doi.org/10.1609/aaai.v35i5.16578>
- [132] H. Xue, L. Yang, V. Rajan, W. Jiang, Y. Wei, and Y. Lin. 2021. Multiplex bipartite network embedding using dual hypergraph convolutional networks. In *Proceedings of the Web Conference 2021 (WWW'21)*. ACM, New York, NY, 1649–1660. <https://doi.org/10.1145/3442381.3449954>
- [133] N. Yadati. 2020. Neural message passing for multi-relational ordered and recursive hypergraphs. In *Proceedings of the 34th International Conference on Neural Information Processing Systems (NIPS'20)*. Curran Associates Inc., Red Hook, NY, Article 276.
- [134] N. Yadati, M. Nimishakavi, P. Yadav, V. Nitin, A. Louis, and P. Talukdar. 2019. HyperGCN: A new method for training graph convolutional networks on hypergraphs. In *Advances in Neural Information Processing Systems*, Vol. 32. Curran Associates, Inc.
- [135] N. Yadati, V. Nitin, M. Nimishakavi, P. Yadav, A. Louis, and P. Talukdar. 2020. NHP: Neural hypergraph link prediction. In *Proceedings of the International Conference on Information and Knowledge Management (CIKM'20)*. Association for Computing Machinery, New York, NY, 1705–1714. <https://doi.org/10.1145/3340531.3411870>
- [136] C. Yang, R. Wang, S. Yao, and T. Abdelzaher. 2022. Semi-supervised hypergraph node classification on hypergraph line expansion. In *Proceedings of the 31st ACM International Conference on Information and Knowledge Management (CIKM'22)*. Association for Computing Machinery, New York, NY, 2352–2361. <https://doi.org/10.1145/3511808.3557447>
- [137] D. Yang, B. Qu, J. Yang, and P. Cudre-Mauroux. 2019. Revisiting user mobility and social relationships in LBSNs: A hypergraph embedding approach. In *The World Wide Web Conference (WWW'19)*. Association for Computing Machinery, New York, NY, 2147–2157. <https://doi.org/10.1145/3308558.3313635>
- [138] D. Yang, B. Qu, J. Yang, and P. Cudre-Mauroux. 2020. LBSN2Vec++: Heterogeneous hypergraph embedding for location-based social networks. *IEEE Transactions on Knowledge and Data Engineering* 34 (2020), 1843–1855. <https://doi.org/10.1109/tkde.2020.2997869>
- [139] J. Yang and J. Leskovec. 2015. Defining and evaluating network communities based on ground-truth. *Knowledge Information Systems* 42, 1 (2015), 181–213. <https://doi.org/10.1007/s10115-013-0693-z>

- [140] J. Yi and J. Park. 2020. Hypergraph convolutional recurrent neural network. In *Proceedings of the 26th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining (KDD'20)*. Association for Computing Machinery, New York, NY, 3366–3376. <https://doi.org/10.1145/3394486.3403389>
- [141] C. Yu, C. Tai, T. Chan, and Y. Yang. 2018. Modeling multi-way relations with hypergraph embedding. In *Proceedings of the ACM International Conference on Information and Knowledge Management (CIKM'18)*. ACM, New York, NY, 1707–1710. <https://doi.org/10.1145/3269206.3269274>
- [142] J. Yu, H. Yin, J. Li, Q. Wang, N. Q. V. Hung, and X. Zhang. 2021. Self-supervised multi-channel hypergraph convolutional network for social recommendation. In *Proceedings of the Web Conference 2021 (WWW'21)*. ACM, New York, NY, 413–424. <https://doi.org/10.1145/3442381.3449844>
- [143] Z. Yu, F. Huang, X. Zhao, W. Xiao, and W. Zhang. 2020. Predicting drug–disease associations through layer attention graph convolutional network. *Briefings in Bioinformatics* 22, 4 (2020). <https://doi.org/10.1093/bib/bbaa243>
- [144] H. Yuan and Y. Y. Tang. 2015. Learning with hypergraph for hyperspectral image feature extraction. *IEEE Geoscience and Remote Sensing Letters* 12, 8 (2015), 1695–1699. <https://doi.org/10.1109/LGRS.2015.2419713>
- [145] E. Zangerle, M. Pichl, W. Gassler, and G. Specht. 2014. #nowplaying music dataset: Extracting listening behavior from Twitter. In *Proceedings of the 1st International Workshop on Internet-Scale Multimedia Management (WISMM'14)*. Association for Computing Machinery, New York, NY, 21–26. <https://doi.org/10.1145/2661714.2661719>
- [146] J. Zhang, M. Gao, J. Yu, L. Guo, J. Li, and H. Yin. 2021. Double-scale self-supervised hypergraph learning for group recommendation. In *Proceedings of the International Conference on Information and Knowledge Management (CIKM'21)*. Association for Computing Machinery, New York, NY, 2557–2567. <https://doi.org/10.1145/3459637.3482426>
- [147] R. Zhang, Y. Zou, and J. Ma. 2020. Hyper-SAGNN: A self-attention based graph neural network for hypergraphs. In *International Conference on Learning Representations (ICLR'20)*.
- [148] V. W. Zheng, B. Cao, Y. Zheng, X. Xie, and Q. Yang. 2010. Collaborative filtering meets mobile recommendation: A user-centered approach. In *Proceedings of the 24th AAAI Conference on Artificial Intelligence (AAAI'10)*. AAAI Press, 236–241. <https://doi.org/10.5555/2898607.2898645>
- [149] D. Zhou, J. Huang, and B. Schölkopf. 2007. Learning with hypergraphs: Clustering, classification, and embedding. In *Proceedings of Neural Information Processing Systems*. 1601–1608.
- [150] Y. Zhu, Z. Guan, T. Tan, H. Liu, D. Cai, and X. He. 2016. Heterogeneous hypergraph embedding for document recommendation. *Neurocomputing* 216 (2016), 150–162. <https://doi.org/10.1016/j.neucom.2016.07.030>
- [151] Y. Zhu and H. Zhao. 2022. Hypernetwork representation learning with the set constraint. *Applied Sciences* 12, 5 (2022). <https://doi.org/10.3390/app12052650>